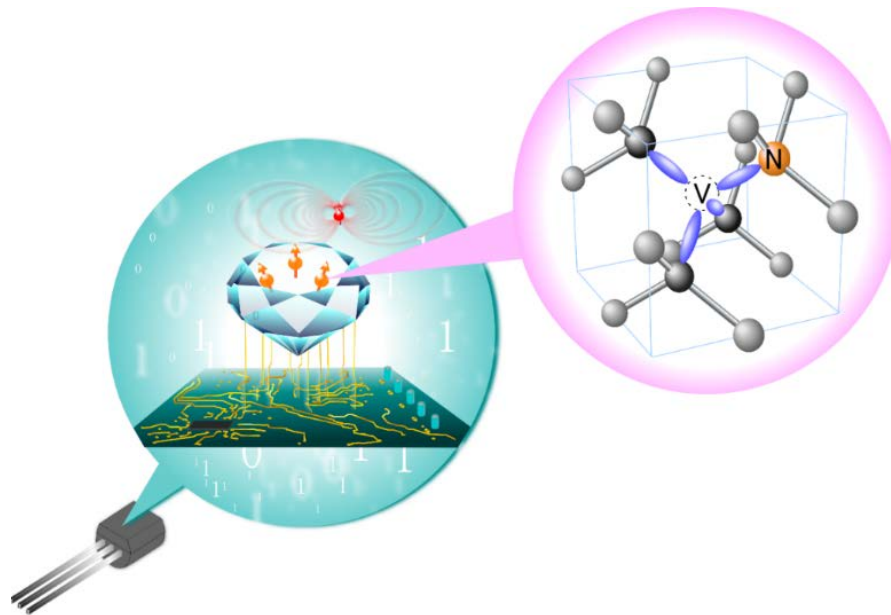


# Nitrogen-Vacancy centers in diamond for quantum sensing

Norikazu MIZUOCHI

Institute for Chemical Research, Kyoto University



1. Overview: Quantum sensor, NV center in diamond
2. Characteristics of NV centers for sensor  
     $\sim$  Why can we improve sensitivity and spatial resolution?  $\sim$
3. How to measure? (Magnetic field, electric field, temperature)
4. Expected applications
5. Our recent studies

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# Quantum science and technology

Quantum computers, Quantum cryptography

Quantum sensors

capitalize on the central weakness of quantum systems, their strong sensitivity to external disturbances.

# Quantum sensor : Definition

C. L. Degen, F. Reinhard, P. Cappellaro, Rev. Mod. Phys., 89, 035002 (2017).

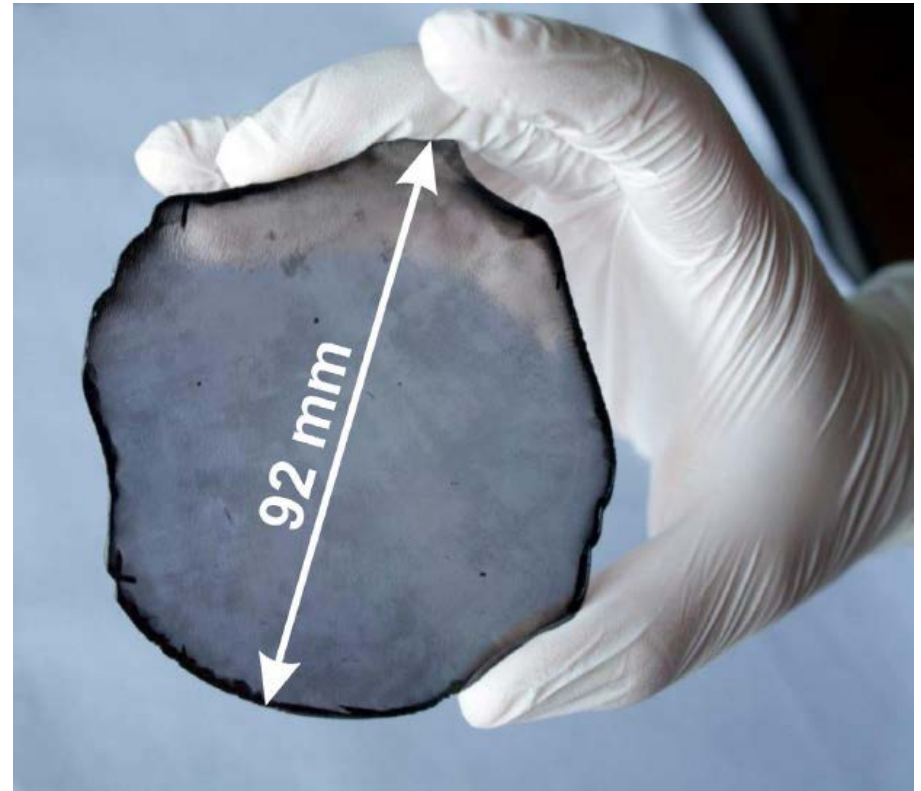
1. Use of a quantum object to measure a physical quantity.  
The quantum object is characterized by **quantized energy levels**. (ex. electronic, magnetic or vibrational states of superconducting or spins, neutral atoms, or trapped ions)  
Close to applications.
2. Use of **quantum coherence** to measure a physical quantity.  
(ex. Spin coherence of NV centers, ...)  
Close to applications. Higher sensitivity and dynamic range than 1.
3. Use of **quantum entanglement** to improve the sensitivity or precision of a measurement, beyond what is possible classically.  
More stringent and a truly quantum definition. Use of it is the ultimate goal but so far, it is difficult to generate, ...

# Experimental implementations of high sensitive quantum sensors.

- Superconducting quantum interference devices (SQUID)
- Atomic vapors or atomic clocks
- Solid-state spins
- ...



Synthetic Diamond  
(CVD, HPHT)  
Commercially available  
(4-10 mm□, <http://www.e6.com/>)



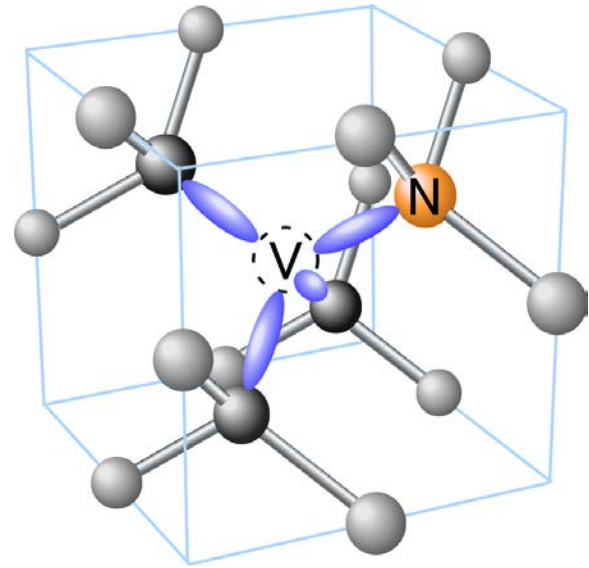
Hetero-epi, CVD,  
single crystal

Scientific reports 7:44462 (2017)  
doi:10.1038/srep44462

The diamond will lose its value as gem stones, but its excellent characters is interested by scientists.

# NV center in diamond

Impurities/defects  
cause Colors!



NV center

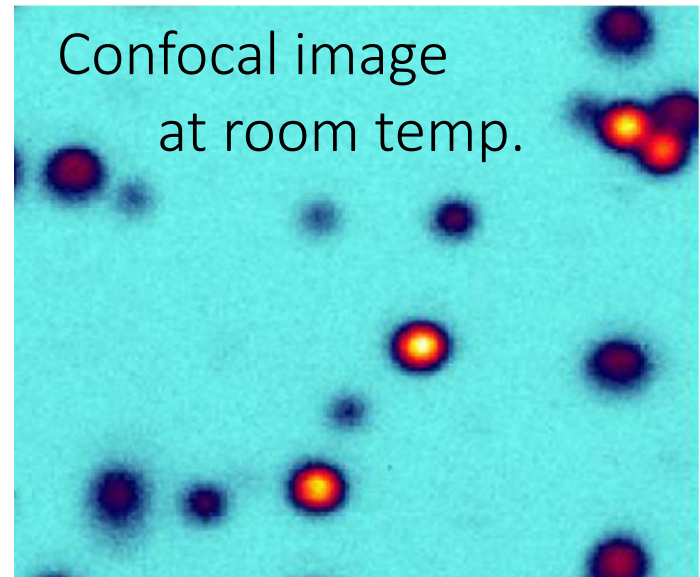
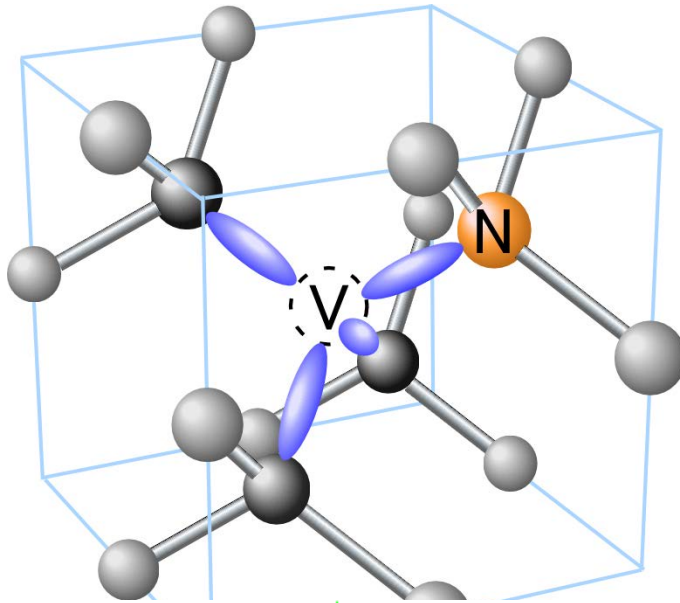
The atomic structure was  
identified by ESR in 1977.

J. H. N. Loubser & J. A. van Wyk, Diamond  
Res., p. 11, 1977



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# NV center in diamond



Confocal image  
at room temp.

Z Rabi oscillation

Coherent Control and detection of Single spin at RT  
Unique character among solid state material

Magnetic sensor: Expected to be as sensitive as a  
superconducting quantum interferometer (SQUID) at room  
temperature!

0

$|1\rangle$

# Characteristics of NV center for sensing

11

Magnetic field sensitivity :  $\eta$

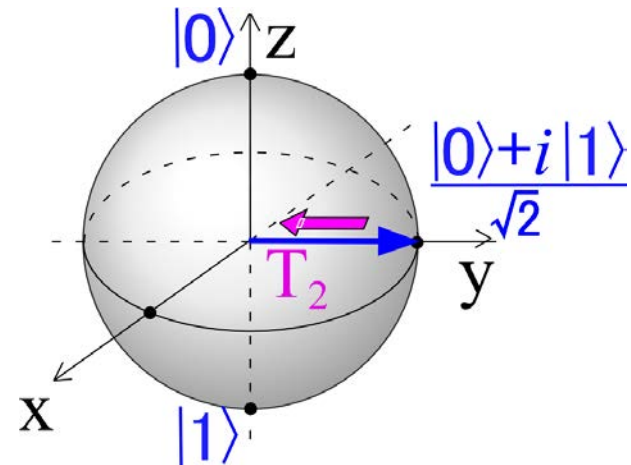
$$\eta \propto \frac{1}{\sqrt{n_{NV}T_2}}$$

$n_{NV}$  : The number of NV

Superposition state

$$|\Psi\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$$

Coherence time ( $T_2$ ) :



Long  $T_2$  : Longest  $T_2$  among solid state electron spins at RT.

Sensing of magnetic field, electric field, temperature, pressure, pH

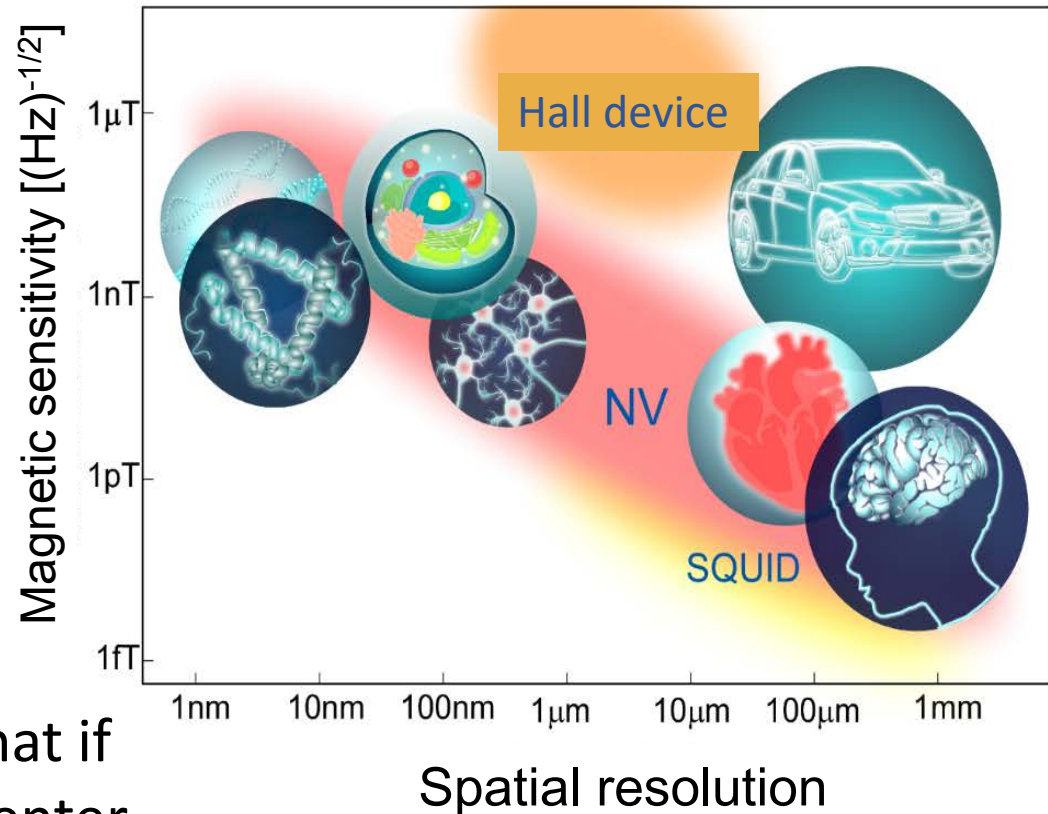
Sensitivity ( $\eta$ )

$$\eta \propto \frac{1}{\sqrt{n_{NV} T_2}}$$

$n_{NV}$  : Number of NV

Not only  $T_2$  but also the number of NV also contributes to the sensitivity.

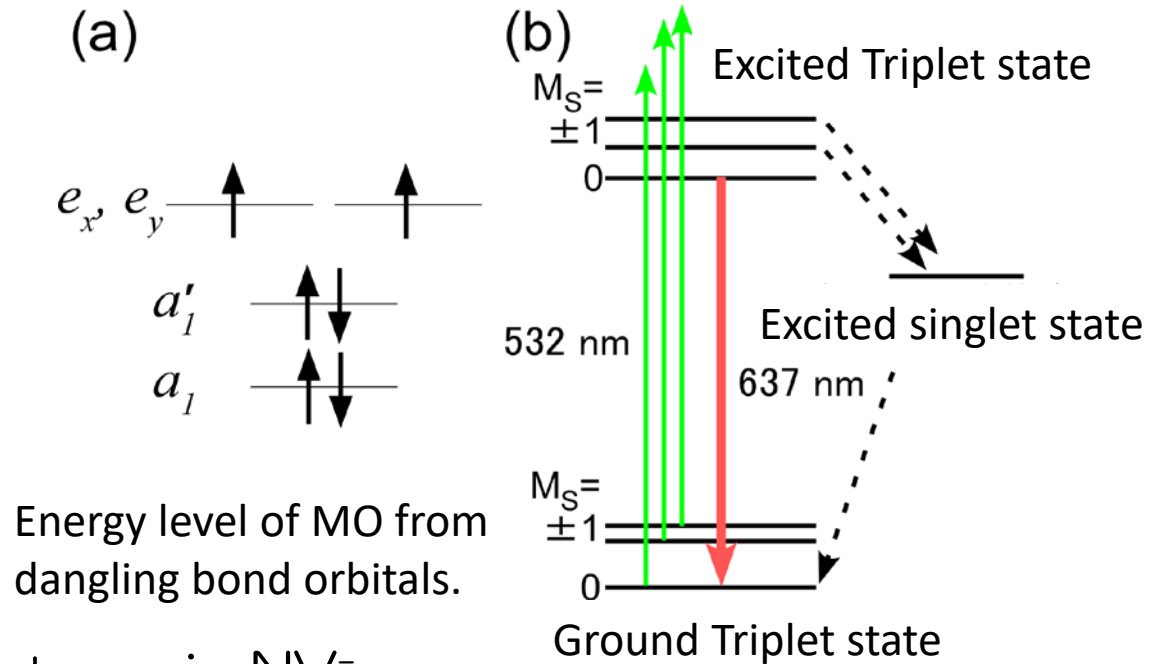
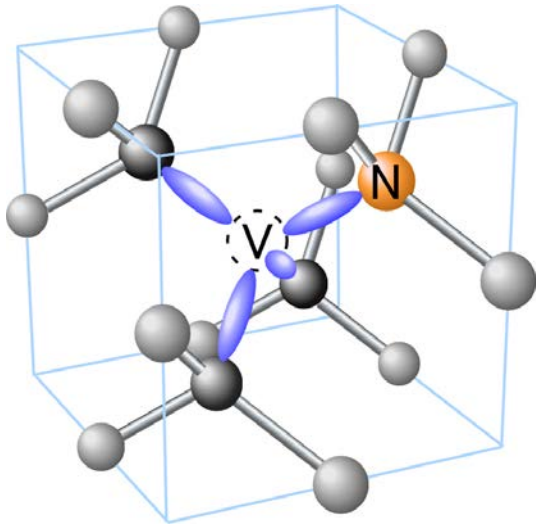
The trade-off relationship is that if the concentration of the NV center increases,  $T_2$  becomes shorter. If the concentration keeps constant and  $n_{NV}$  increases, the spatial resolution decreases.



Mizuochi, OYO BUTSURI, 87, 251-261(2018).

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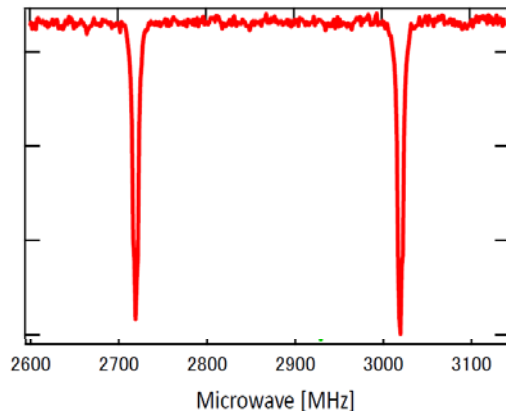
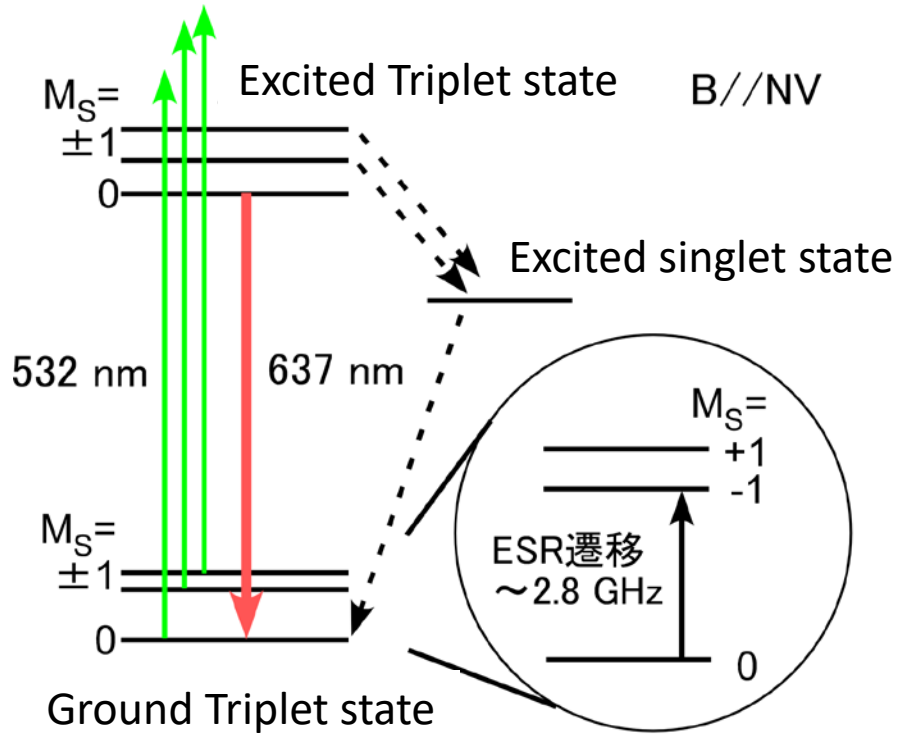
# Why does NV center has ground triplet state ( $S=1$ )?



6 electrons in  $NV^-$

- In diamonds, it is often energetically advantageous to maintain high symmetry.
- According to Pauli exclusion principle, upspins are added to each of the two degenerate levels, and  $S = 1$ !

# Measurement method : Optically detected magnetic resonance (ODMR)



**1: Initialization (To  $M_S = 0$ ):** Laser excitation (532 nm) and spin selective deactivation due to SOC.

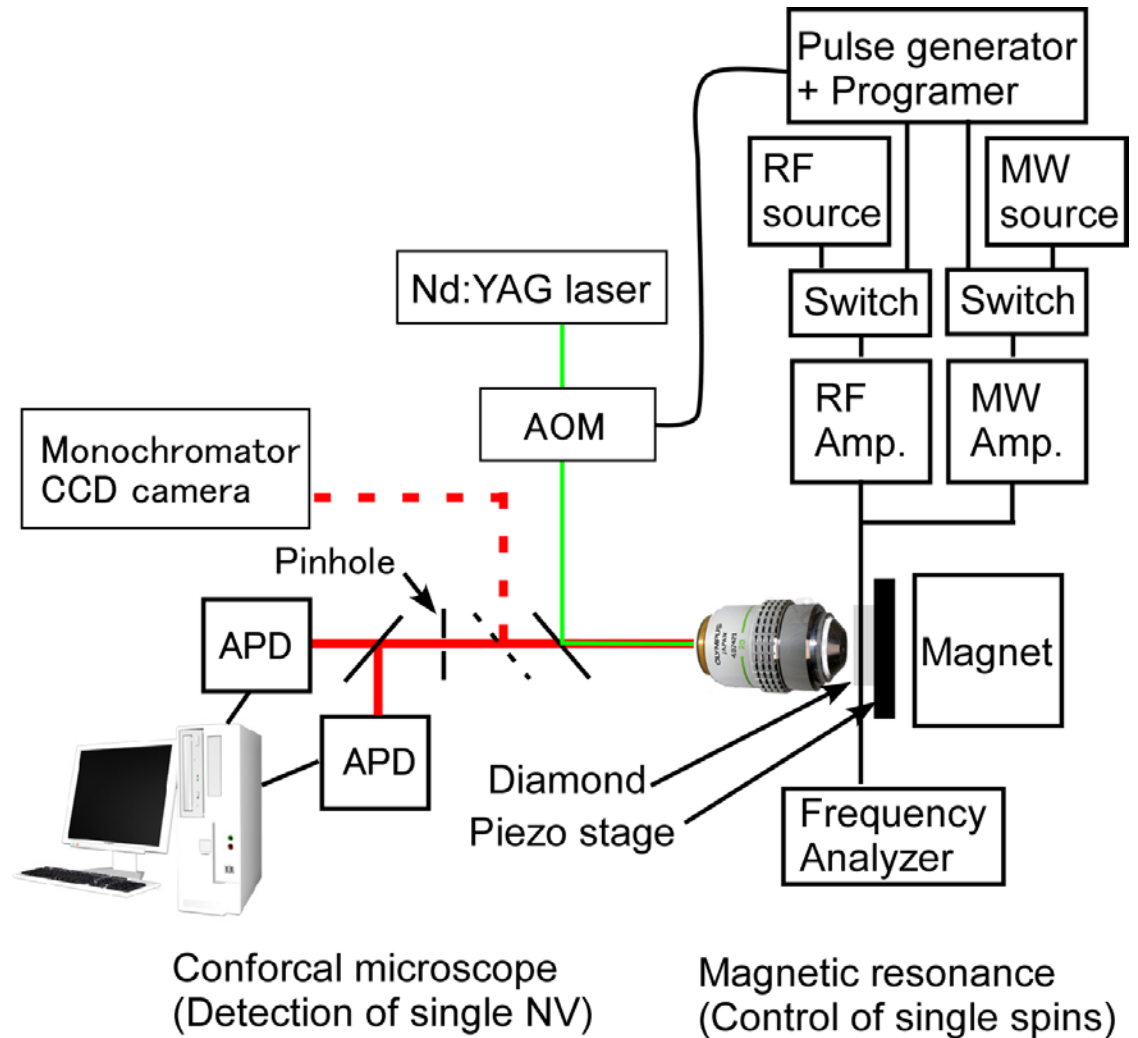
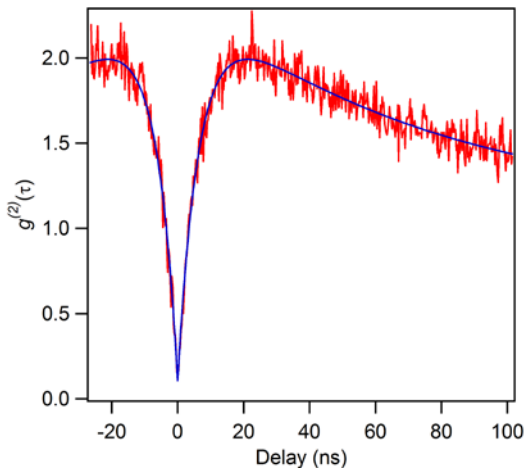
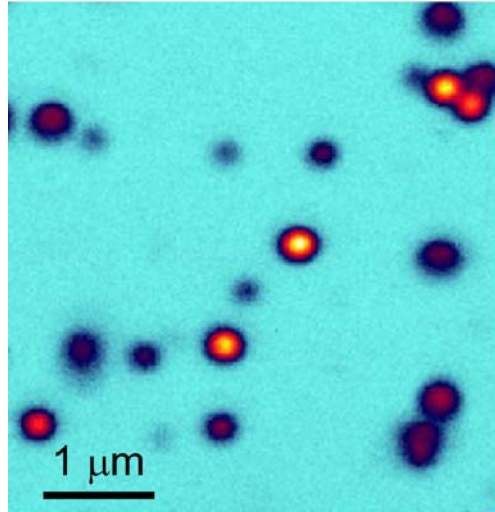
**2: Magnetic resonance (To  $M_S = -1$ )**  
Microwave irradiation to Zero-field splitting (dipolar-dipolar interaction) = 2.87 GHz

**3: Optical detection:**

Laser excitation (532 nm) and detection of change of fluorescence.

# Measurement setup of individual centers

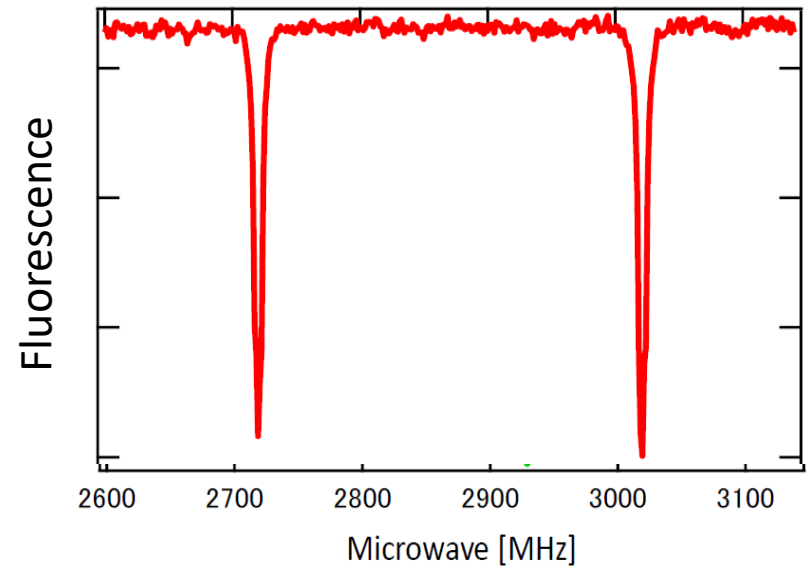
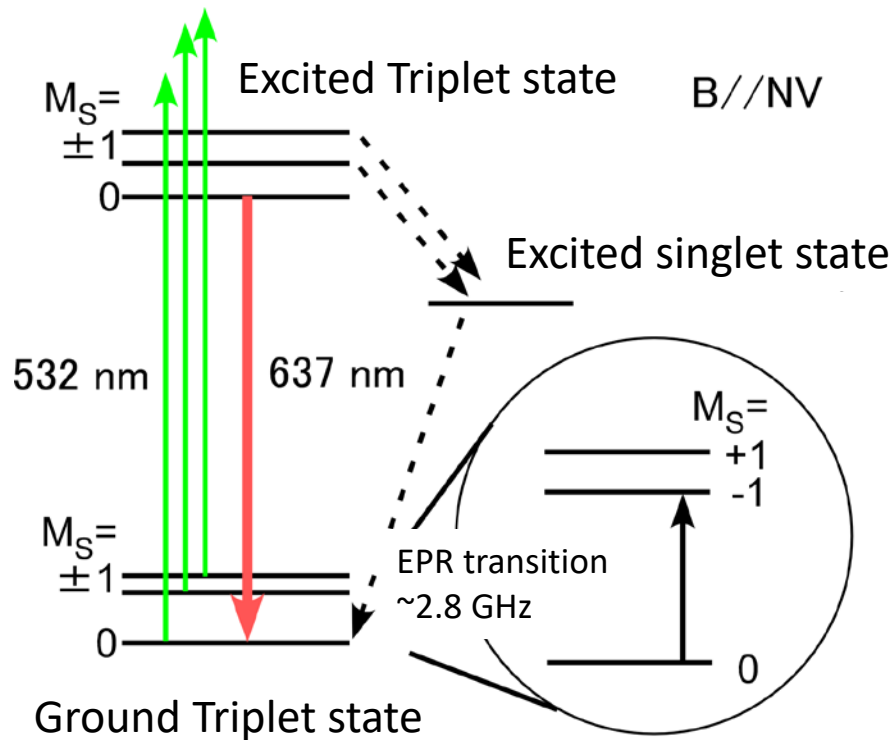
## Confocal microscope with magnetic resonance system



Measurement using a piezostage and observe each single emission center



# How to sense the magnetic field?



ODMR spectrum of NV center

The resonance freq. of the ODMR signal shifts according to the magnitude of the magnetic field. Measurement of the magnetic field from the shift!

The narrower the line width, the smaller the shift can be detected. Namely, the sensitivity improves! (The longer  $T_2$ , the narrower the line width! )

Magnetic field, temperature, electric field, and pressure can be measured!

## Spin Hamiltonian

$$H_{gs} \cong \underbrace{\mu_B g_e \mathbf{S} \cdot \mathbf{B}}_{\text{Magnetic field}} + \underbrace{\frac{hD_{gs} \left[ S_z^2 - \frac{1}{3} S(S+1) \right]}{\text{Temperature Stress}}}_{\text{Spin-spin interaction (dipolar int.)}} - \underbrace{d_{gs}^{\perp} \left[ E_x (S_x S_y + S_y S_x) + E_y (S_x^2 - S_y^2) \right]}_{\text{Electric field}}$$

Demonstrated high sensitivity (room temperature)

Temperature (single)

$$5 \text{ mK}/\sqrt{Hz}$$

Neumann, et al., Nano Lett. 2013

Stress

$$0.6 \text{ MPa}/\sqrt{Hz}$$

Doherty, et al., PRL 2014.

Electric field (single)

$$202 \text{ V/cm}/\sqrt{Hz}$$

Dolde, et al., Nat. Phys. 2011.

# Magnetic sensor sensitivity using the NV center

Ensemble (RT)

$$B_{AC} \sim 0.9 \text{ pT Hz}^{-1/2}$$

PRX 2015

Spatial resolution :  $50 \text{ } \mu\text{m} \times 50 \text{ } \mu\text{m} \times 0.5 \text{ mm}$

Ensemble (RT)

$$B_{DC} \sim 15 \text{ pT Hz}^{-1/2}$$

PNAS 2017

Single (RT)

$$B_{AC} = 9.1 \text{ nT Hz}^{-1/2}$$

Nature Commun. 2019

Single (RT)

$$B_{DC} = 10 \text{ nT Hz}^{-1/2}$$

Nature Commun. 2019

Magnetic field sensitivity (Minimum detectable B) :  $\eta$

$$\eta \propto \frac{1}{C \sqrt{n_{NV} \tau T_2}}$$

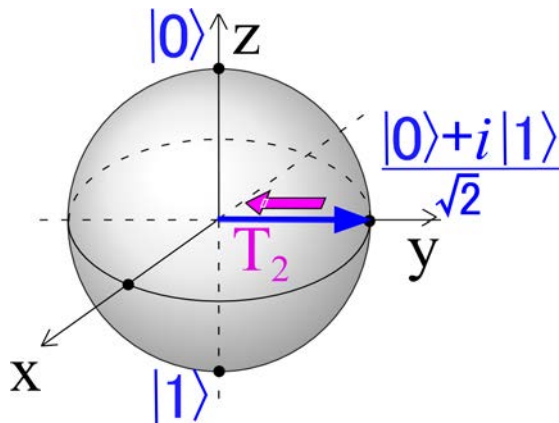
$C$  : readout contrast

$n_{NV}$  : The number of NV

$\tau$  : Measurement time

# Phase measurement

We can obtain information such as magnetic field from the phase of coherence!



Coherence is generated by 90 degree pulse. After that, when the magnetic field from the outside changes, the coherence begins to rotate in the xy plane when viewed in the rotating coordinate system. Information on the magnetic field from the outside can be obtained from the phase.

Magnetic field sensitivity (Minimum detectable B) :  $\eta$

$$\eta \propto \frac{1}{C \sqrt{n_{NV} \tau T_2}}$$

$C$  : readout contrast

$n_{NV}$  : The number of NV

$\tau$  : Measurement time

L. M. Pham, et. al., Phys. Rev. B **86**, 121202 (2012)

# Accuracy of phase measurement

$$\phi = \phi_0 \pm \Delta\phi$$

The smaller  $\Delta\phi$ , the better the accuracy.

Classical measurement (when measuring with  $n$  spins)

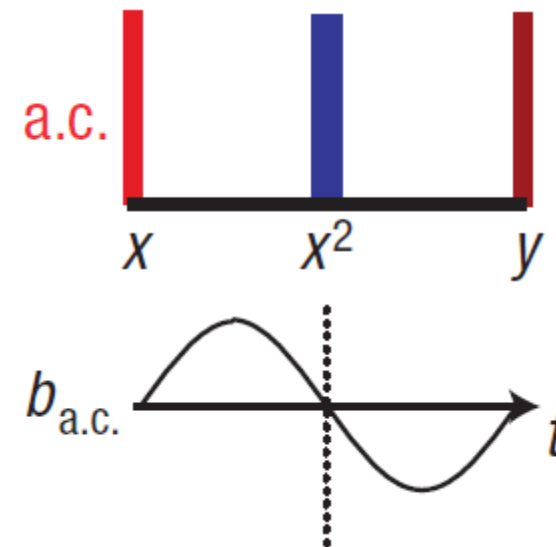
Limitation of accuracy:  $\Delta\phi \approx \frac{1}{\sqrt{n}}$

Quantum measurement (when measuring using the quantum entangled state with  $n$  spins)

Limitation of accuracy:  $\Delta\phi \approx \frac{1}{n}$

# AC magnetic field detection

Echo - type sequence ( $\pi/2 - \pi - \pi/2$ )



$$\delta\phi = \left(\frac{g\mu_B}{\hbar}\right) \left[ \int_0^{\tau/2} b(t)dt - \int_{\tau/2}^0 b(t)dt \right]$$

$$b(t) = b \sin(\nu t + \phi_0) \quad \nu: \text{signal field frequency}$$

$\phi_0$ : initial phase

$$\delta\phi = \left(\frac{g\mu_B}{\hbar}\right) b\tau f(\nu\tau, \phi_0)$$

$$f(\nu\tau, \phi_0) = \left( \sin^2(x/4) \cos \frac{\left(\frac{x}{2} + \phi_0\right)}{x} / 4 \right)$$

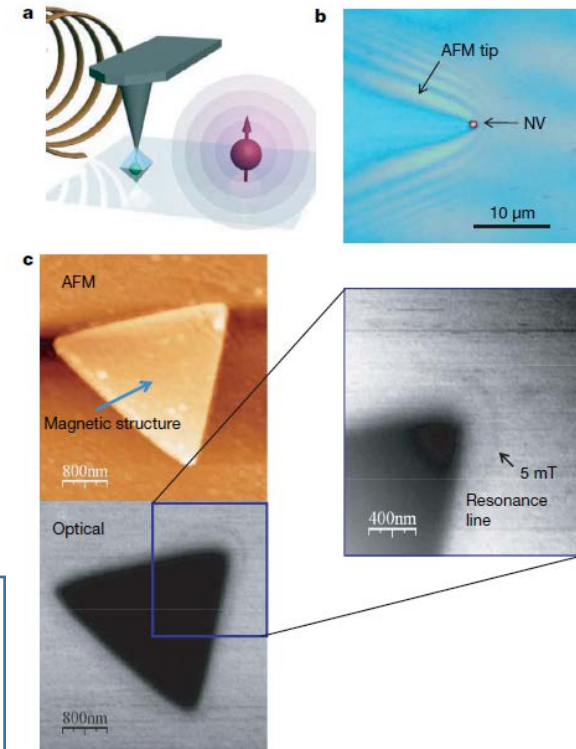
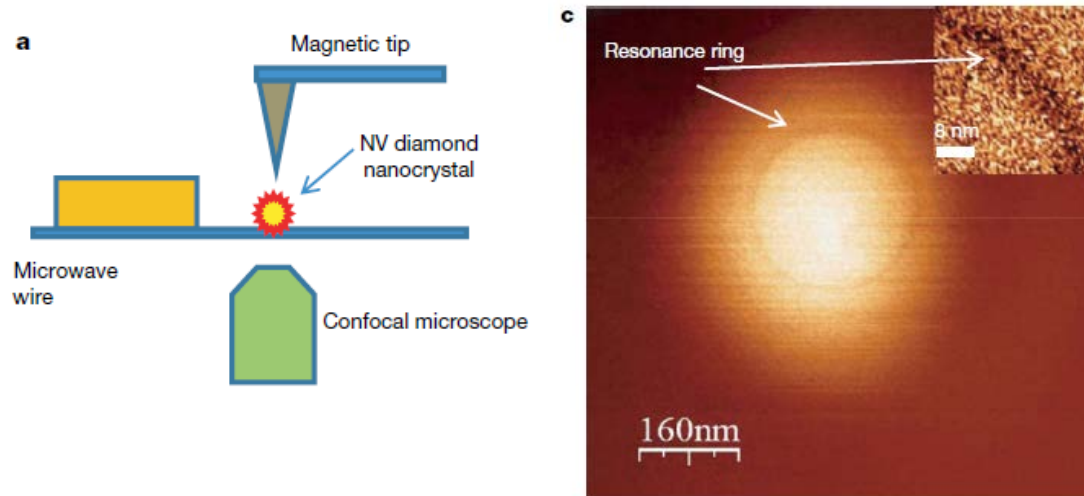
Optimum condition

$$\tau = 2\pi/\nu \text{ and } \phi_0 = 0$$

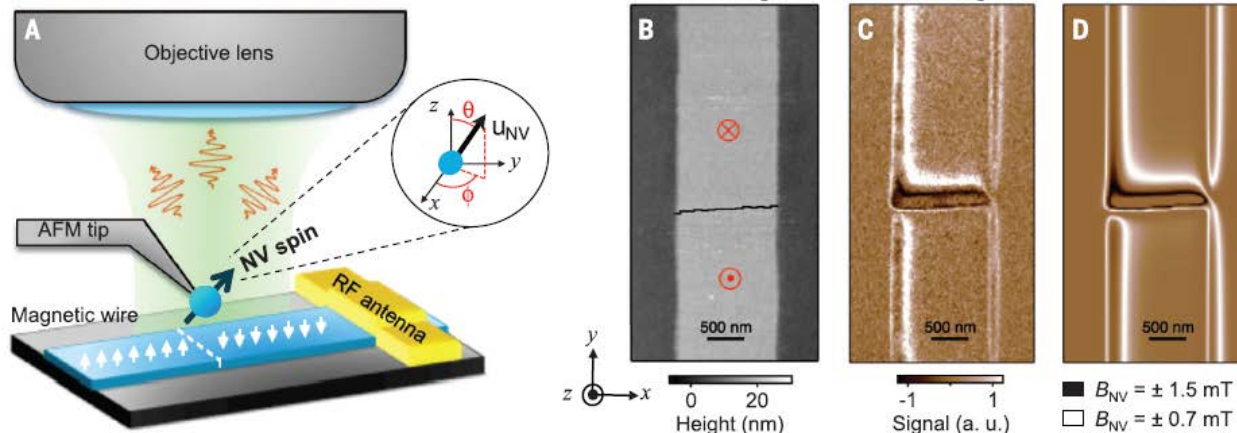
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# High magnetic field sensitivity and high spatial resolution

Nature, 455, 648, 2008



Science 2014





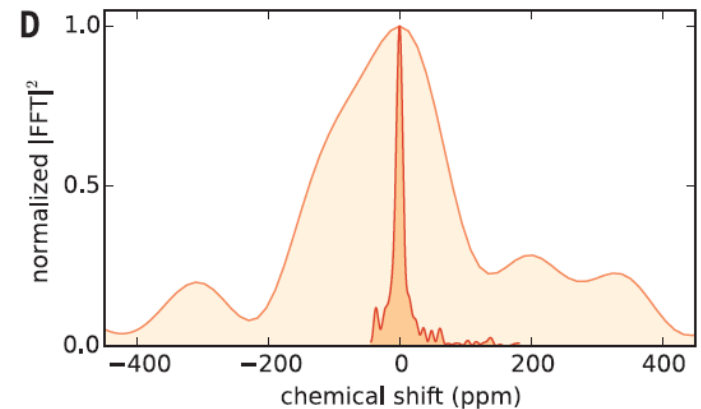
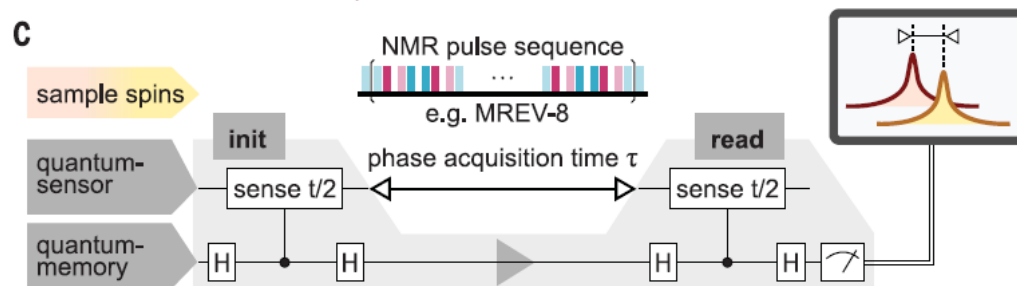
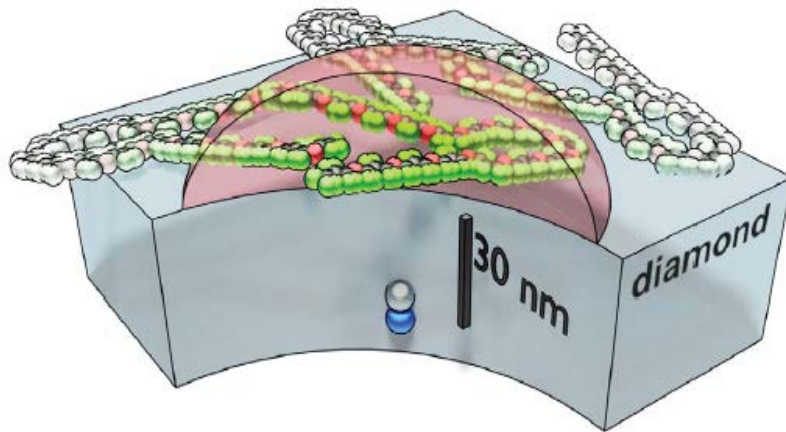
## AC magnetic field sensing

## nanometer scale NMR

N. Aslam, et al., Science, 357, 65 (2017)

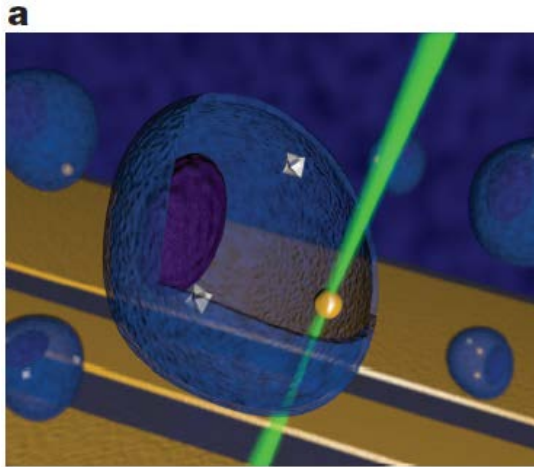
The nuclear spin of a molecule placed on the diamond surface is measured by the NV center.

To structural analysis of  
small amounts of molecules

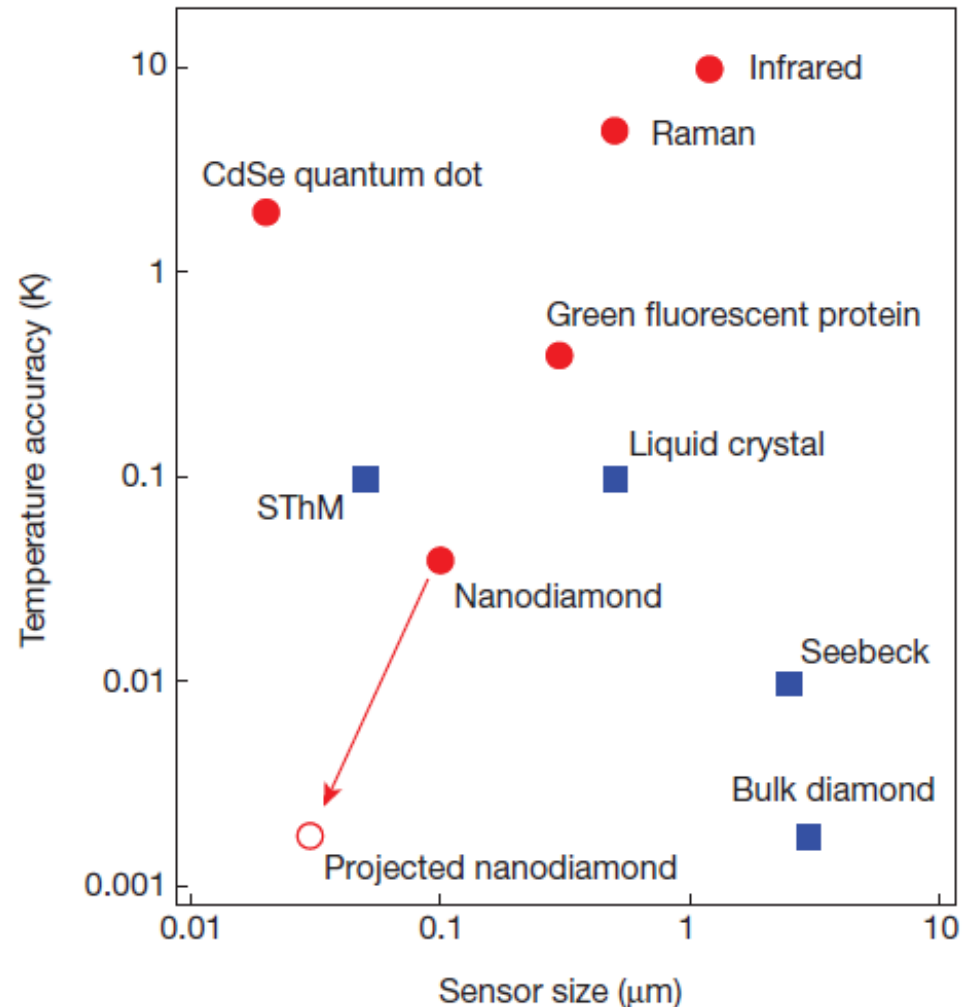
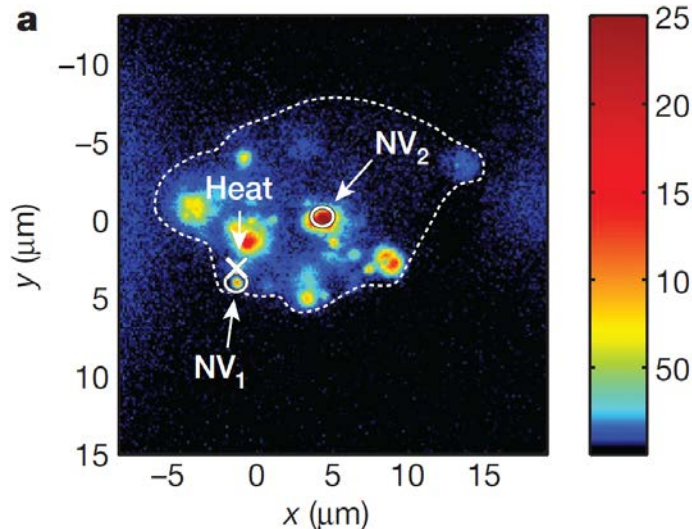


# Intracellular nanometer scale thermometer

Kucsko et al., Nature 2013



Sensitivity :  $9 \text{ mK/Hz}^{1/2}$  (Bulk)  
 Nano diamond : 200 nm



# Testing Fundamental Physics by using NV centers

“Searching for an exotic spin-dependent interaction with a single electron-spin quantum sensor”,

X. Rong, J. Du et al., *Nature Communications*, (2018) 9, 739.

“Testing quantum gravity by nanodiamond interferometry with nitrogen-vacancy centers”

A. Albrecht, A. Retzker, M. B. Plenio, *Physical Review A* 90, 033834 (2014).

Related study: “Constraints on bosonic dark matter from ultralow-field nuclear magnetic resonance”,

A. Garcon, D. Budker et al., *Science Advances* 2019; 5 : eaax4539.

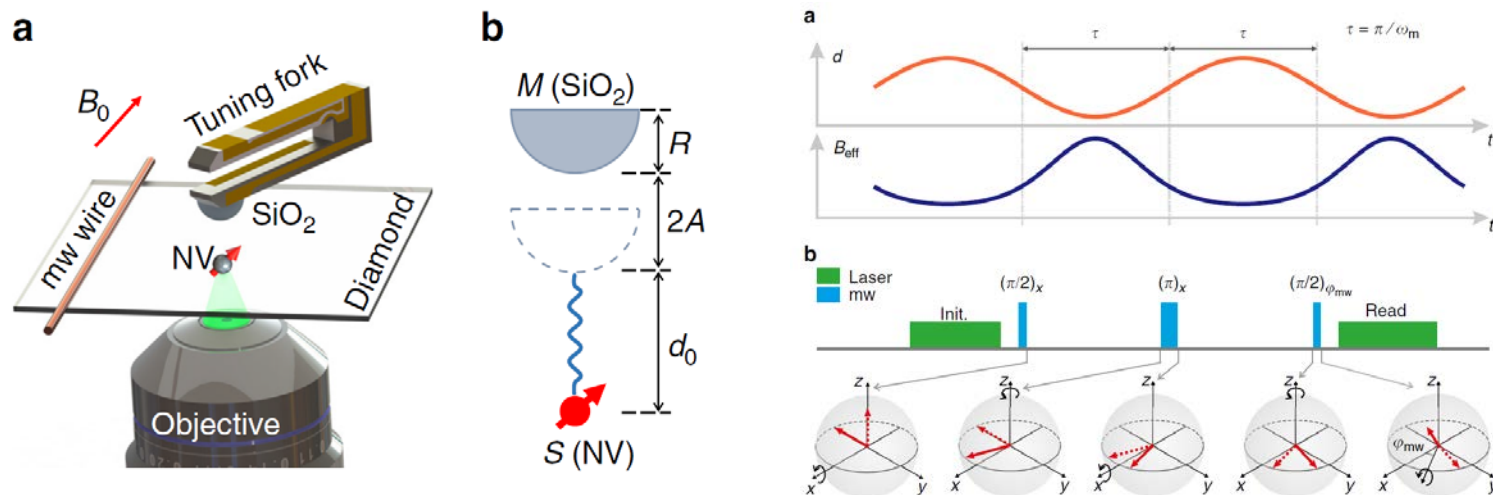
“Searching for an exotic spin-dependent interaction with a single electron-spin quantum sensor”,  
X. Rong, J. Du et al., *Nature Communications*, (2018) 9, 739.

The axion-mediated monopole–dipole interaction can be described as

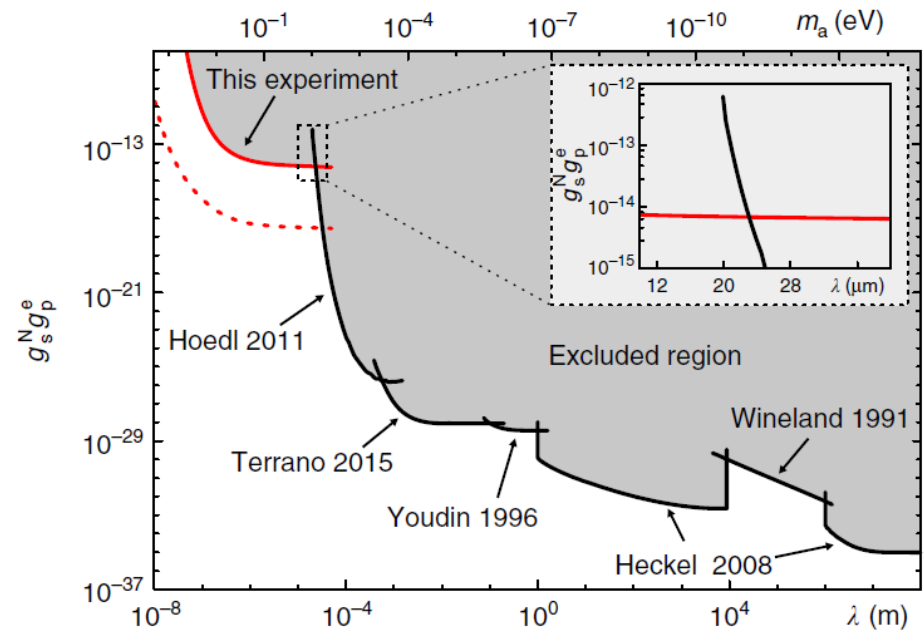
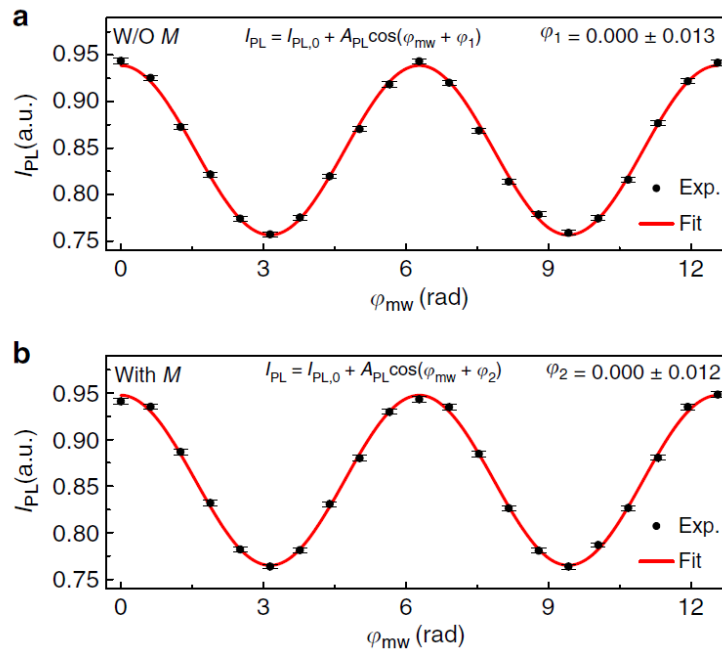
$$V_{\text{sp}}(\mathbf{r}) = \frac{\hbar^2 g_s^N g_p^e}{8\pi m} \left( \frac{1}{\lambda r} + \frac{1}{r^2} \right) e^{-\frac{r}{\lambda}} \boldsymbol{\sigma} \cdot \mathbf{e}_r,$$

Such interaction is equivalent to the Hamiltonian of the electron spin in an effective magnetic field  $\mathbf{B}_{\text{sp}}(\mathbf{r})$  arising from the nucleon,

$$\mathbf{B}_{\text{sp}}(\mathbf{r}) = \frac{\hbar g_s^N g_p^e}{4\pi m \gamma} \left( \frac{1}{\lambda r} + \frac{1}{r^2} \right) e^{-\frac{r}{\lambda}} \mathbf{e}_r,$$

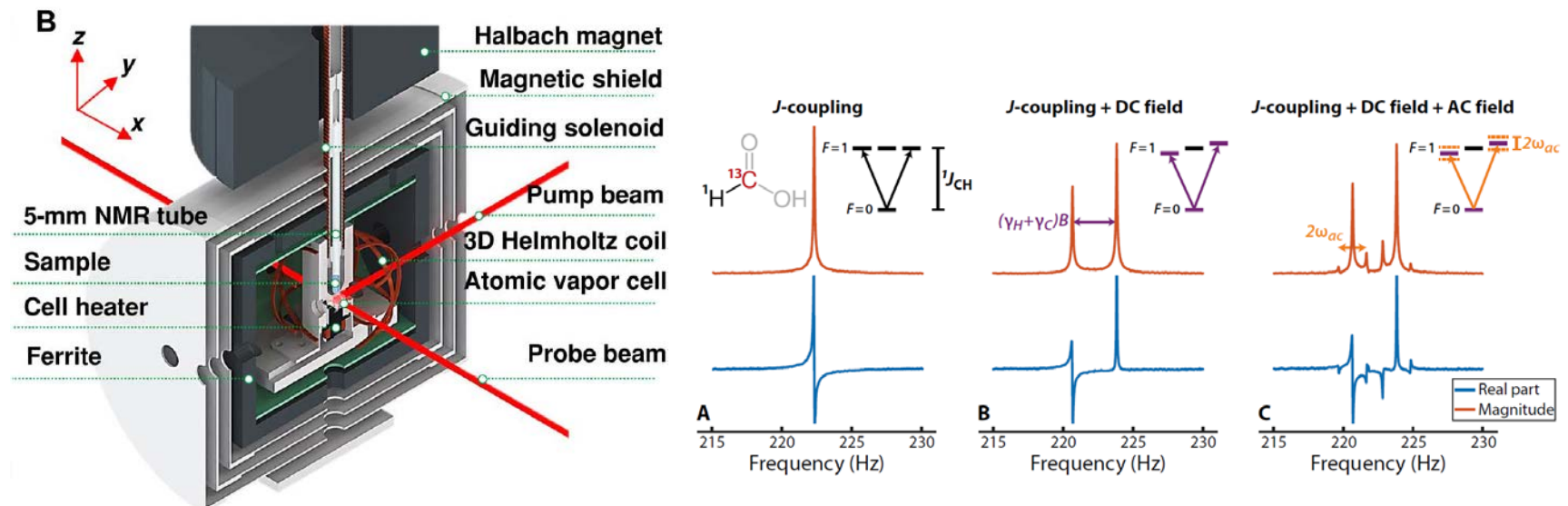


“Searching for an exotic spin-dependent interaction with a single electron-spin quantum sensor”,  
 X. Rong, J. Du et al., *Nature Communications*, (2018) 9, 739.



“Constraints on bosonic dark matter from ultralow-field nuclear magnetic resonance”,  
 A. Garcon, D. Budker et al., *Science Advances* 2019; 5 : eaax4539.

Detected from NMR through coupling of dark matter and nuclear spin



Sensitivity of the sensor:  $10 \text{ fT}/(\text{Hz})^{1/2}$ . 50 microL.

No dark matter signal was detected above background,  
 establishing new experimental bounds for dark matter bosons  
 with masses ranging from  $1.8 \times 10^{-16}$  to  $7.8 \times 10^{-14}$  eV.

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  - Ultra-long coherence times among room-temperature solid-state spins
  - Ultra-high dynamic range quantum measurements retaining its sensitivity

# $T_2$ of electron spin of NV centers at RT

$T_2$  (electron spin in natural abundance of  $^{13}\text{C}$  ( $I=1/2$ ))

2003    50  $\mu\text{s}$     T. A. Kennedy, et al., APL, 2003

2006    200  $\mu\text{s}$     L. Childress, et al., Science, 2006

350  $\mu\text{s}$     T. Gaebel, et al., Nature physics, 2006

2009    650  $\mu\text{s}$     N. Mizuochi, et al., PRB, 2009

2010    630  $\mu\text{s}$     R. L. Walsworth et al., PRB 2010

Longest  $T_2$  in natural abundance of  $^{13}\text{C}$ .

Due to suppression of paramagnetic impurities

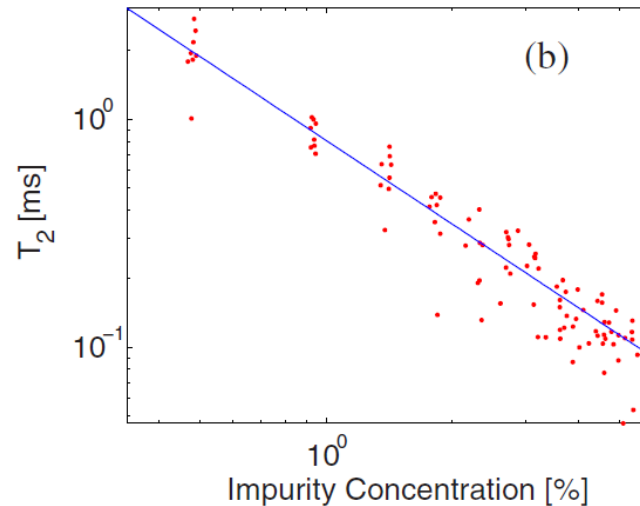
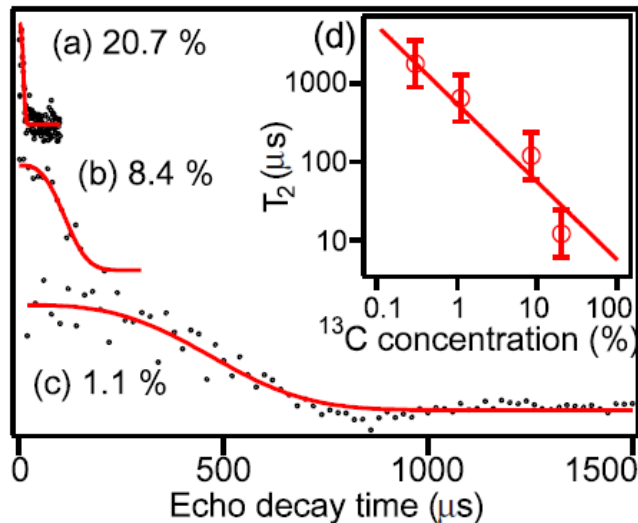
$T_2$  (electron spin in  $^{12}\text{C}$  ( $I=0$ ) enriched diamond: 99.7%)

2009    1.8 ms    G. Balasubramanian, et al., Nat. Mater. 2009.

Due to reduction of nuclear spins



# How to extend $T_2$ ?



N. Mizuochi, et al., PRB, 80, 041201(R) (2009).

J. R. Maze, et al., PRB **78**, 094303 (2008).

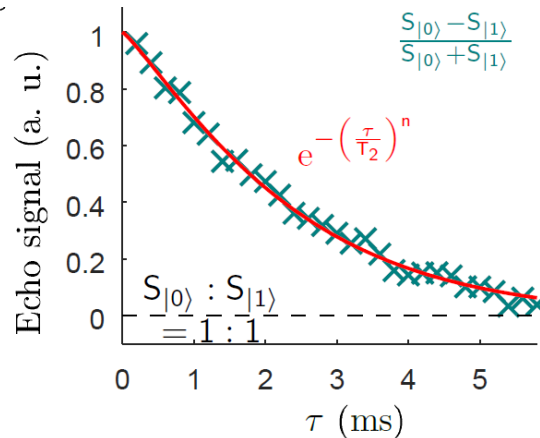
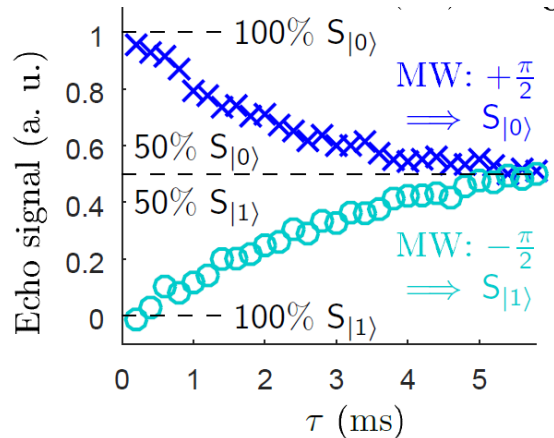
$^{13}\text{C}$  (0.001 %,  $^{12}\text{C}$  = 99.999 %) methane is available:

If  $T_2$  is only limited by  $^{13}\text{C}$  nuclear spin (0.001%),  $T_2$  should be longer than 600 ms.

In diamond with extremely low  $^{13}\text{C}$  (0.001%),  $T_2$  is not limited by noises from nuclear spins.

Suggest: The remaining noise source may be paramagnetic impurities or defects. How to remove them?

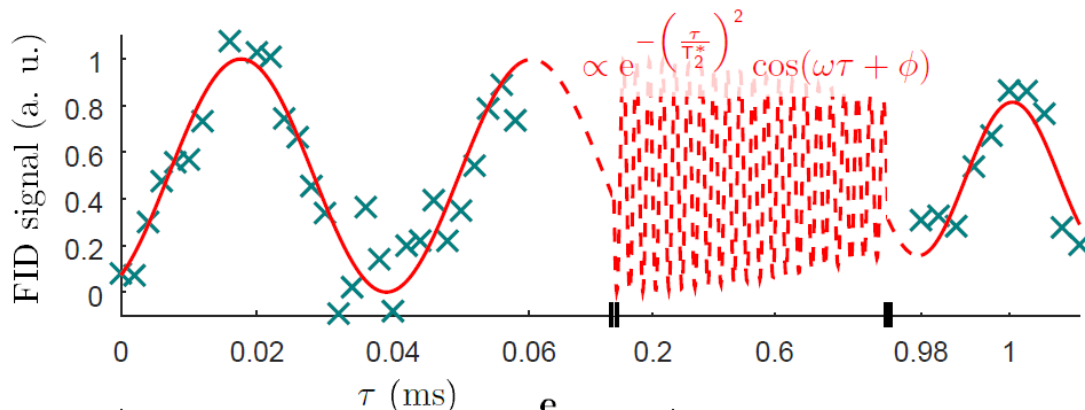
# Ultra-long coherence times among room-temperature solid-state spins (synthesized at AIST) (Nature Communications, 10, 3766 (2019).)



$$T_2 \approx 2.4 \text{ ms}$$

Previous report:  $T_2 = 1.8 \text{ ms}$ :  
Nature Material 2009

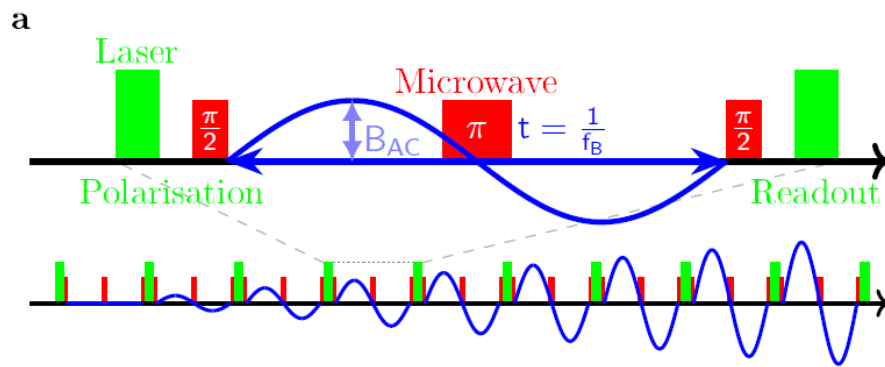
In case without the common mode noise subtraction,  $T_2$  of our NV is estimated to **3.0 ms**.



$$T_2^* \approx 1.5 \text{ ms}$$

Previous report:  $T_2^* = 0.47 \text{ ms}$   
Science 2012

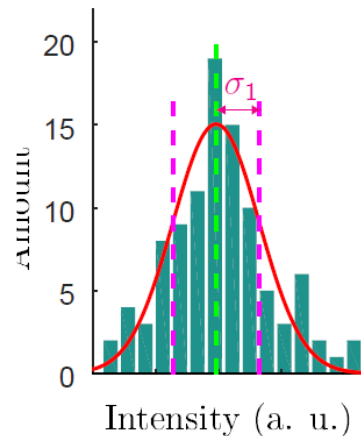
Longest coherence times among solid-state electron spins at room temperature.



Sensitivity:

$$\eta = \delta B_{min} \sqrt{T_{meas}}$$

$$\delta B_{min} = \sigma_B = \frac{\sigma_1}{grad}$$

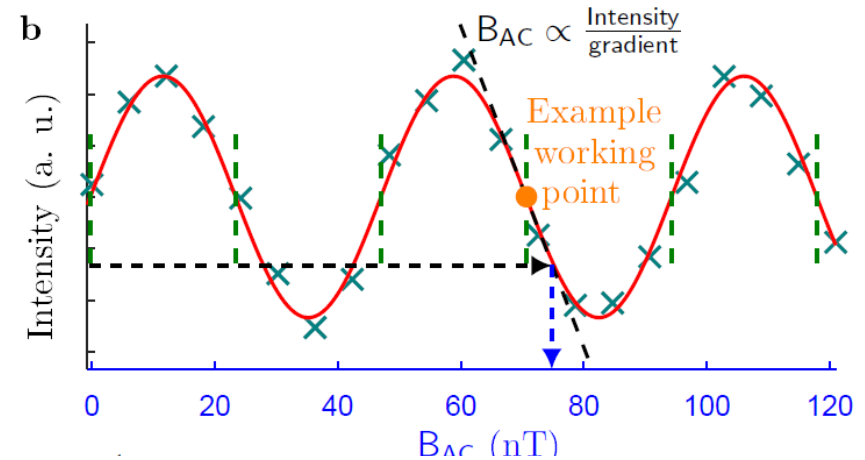


AC magnetic field sensitivity :

$$9.1 \text{ nT}/(\text{Hz})^{1/2}$$

DC magnetic field sensitivity :

$$<10 \text{ nT}/(\text{Hz})^{1/2}$$



Different estimation  
method :  $4.3 \text{ nT}/(\text{Hz})^{1/2}$   
by Nature Mat. 2009

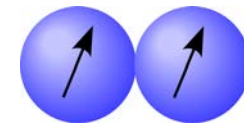
Highest magnetic field sensitivity of single NV at room temperature.

# Effect of P-doped n-type diamond on $T_2$

Phosphorus is one of sources of magnetic noises due to its electron spin. However, the P-doped n-type diamond realizes remarkably long  $T_2$ .

## Non-doped diamond

Multiple vacancies/impurities complexes:  
One of the sources of magnetic noise

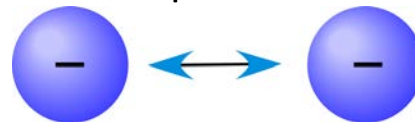


Vacancies/impurities

Vacancy: removable at 600°C. Multiple vacancies/impurities: Stable even at 1,500°C.  
CVD growth temperature is about 900°C.

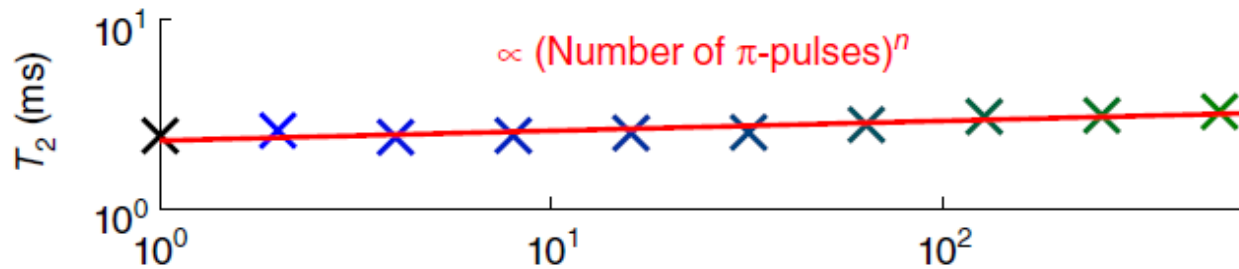
## P-doped n-type diamond

Coulomb repulsion between vacancies/impurities prevents formation of Multiple vacancies/impurities complexes.



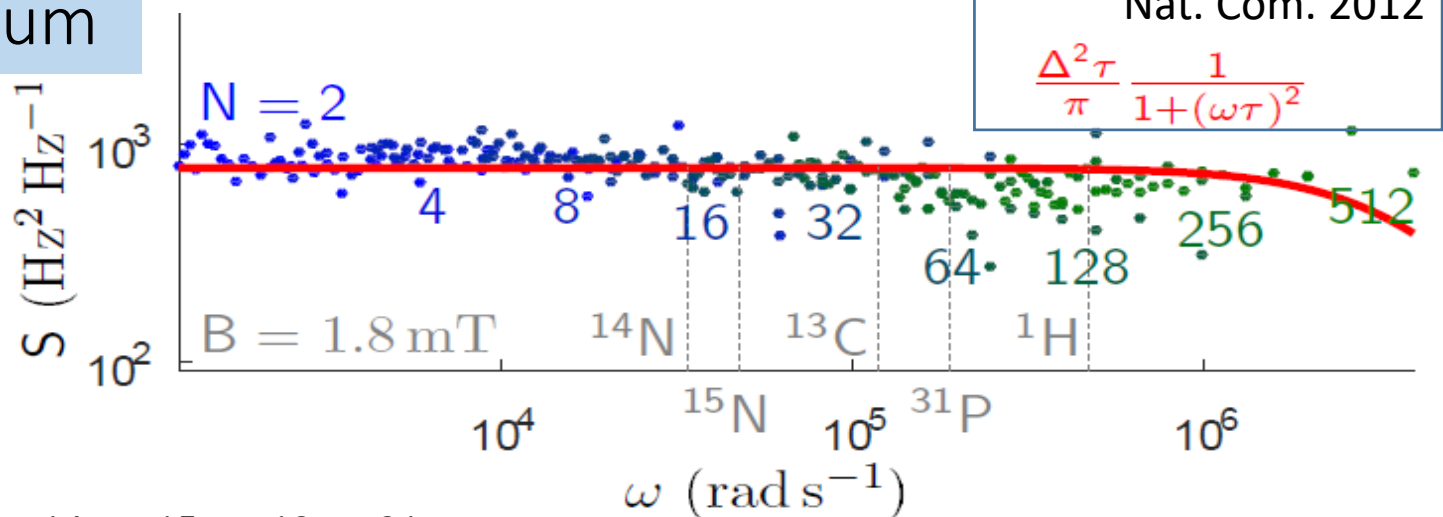
Related research: Model of suppression of multiple vacancies in p-type diamond. F. F. Oliveira, J Wrachtrup, et al., Nature Commun., 8, 15409 (2017).

# About origin of remaining noise source: CPMG dynamical-decoupling sequences



$T_{2dd} = 3.3$  ms  
Still shorter than  
 $T_1$  ( $\sim 6$ ms-7.5 ms)

## Noise spectrum



Nuclear spins of  $^{14}\text{N}$ ,  $^{15}\text{N}$ ,  $^{13}\text{C}$ ,  $^{31}\text{P}$  were not detected.

The minimum density of the paramagnetic defects was derived from  $\Delta$  (under the assumption of dipolar interaction) :  $3 \times 10^{17} \text{ cm}^{-3}$ .

Suggestion: The main noise source is magnetic noises of electron spin.

# Short Summary of first part

- The longest  $T_2^*$  (= 1.5 ms) and  $T_2$  (= 2.4 ms) ever observed in room-temperature solid-state systems.
- The highest magnetic field sensitivities of single NV centers at room temperature.
- The elongation of coherence times in n-type semiconductor diamond paves the way to the development and application of diamond-based quantum-information and sensing devices.

E. D. Herbschleb, H. Kato, Y. Maruyama, T. Danjo, T. Makino, S. Yamasaki, I. Ohki, K. Hayashi, H. Morishita, M. Fujiwara, N. Mizuochi, Ultra-long coherence times amongst room-temperature solid-state spins, *Nature Communications*, **10**, 3766 (2019)

# Ultra-high dynamic range quantum measurements retaining its sensitivity

- Important compared with high sensitive sensors such as SQUID, OPM, MR sensors.
- Interaction between the spins strongly depends on the distance ( $r^3$ ).

Basic quantum sensing protocols cannot simultaneously achieve both a high sensitivity and a large range.

AC field:  $4 \times 10^3$  times (=DR/sensitivity) (RT, Non-adaptive)

A. Lazarev, et al., *Scientific Reports*, 7, 6586 (2017)

DC field:  $< 3 \times 10^5$  times (=DR/sensitivity) (8K, Adaptive,  $B_{\max} = 1.78$  mT )

C. Bonato, et al., *Nature Nanotechnology* 11, 247 (2015)

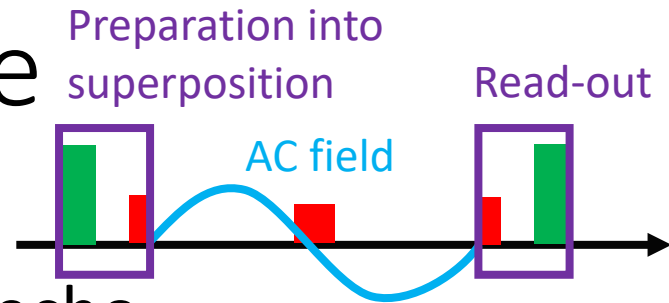
DC field: 130 times (=DR/sensitivity) (Low temp. Non-adaptive)

G. Waldherr, et al., *Nature Nanotechnology* 7, 105 (2011)

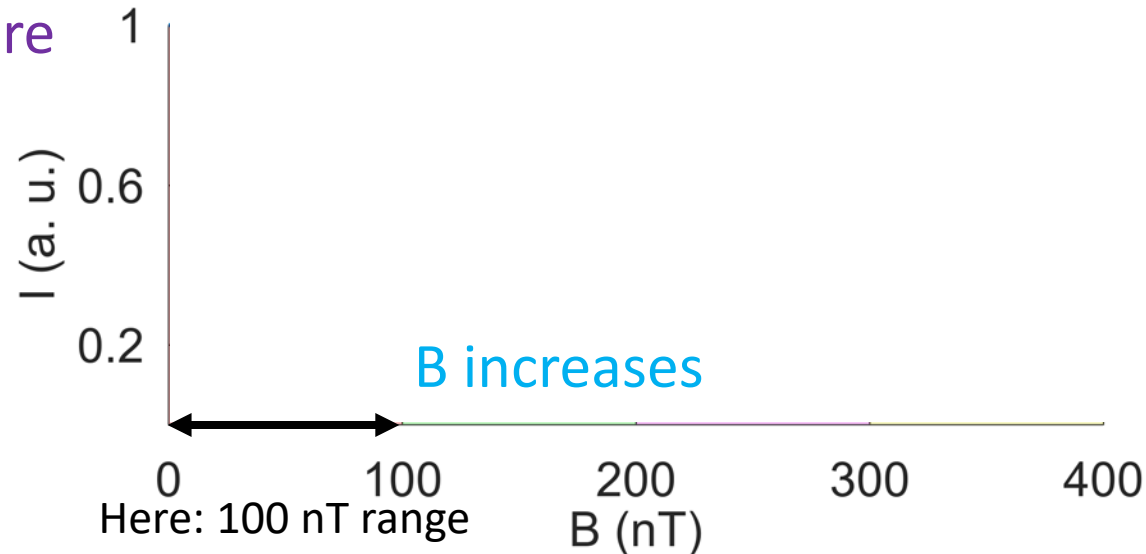
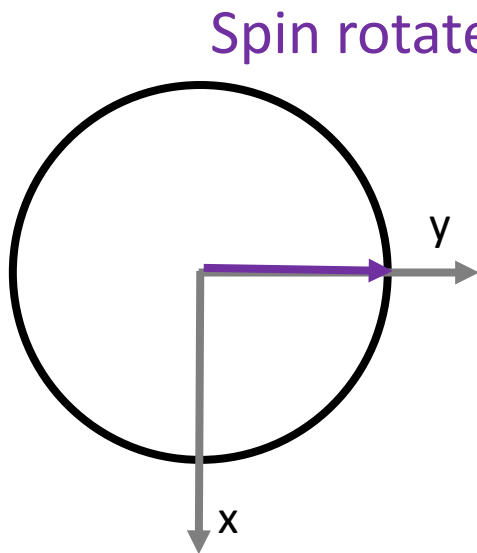
Sensitivity scales as  $\text{sub-}1/T^{0.5}$  by applying different amounts of iterations, as opposed to the  $T^{-1/2}$  of the standard measurement

B increases, spin rotates more

# Problem – limited range



- Standard AC measurement: Hahn-echo sequence with spin
- Limited range due to rotational symmetry





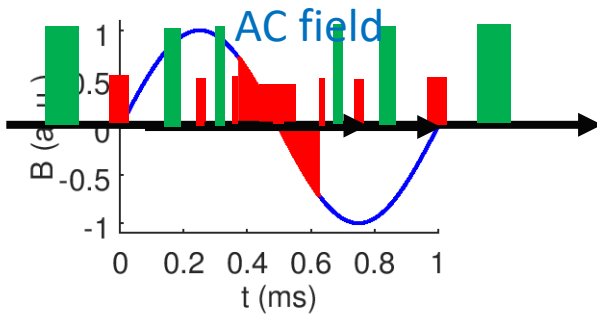
$$\text{sensitivity} \propto \text{uncertainty} \propto \frac{1}{\text{maximum gradient}}$$

# Standard measurement DR

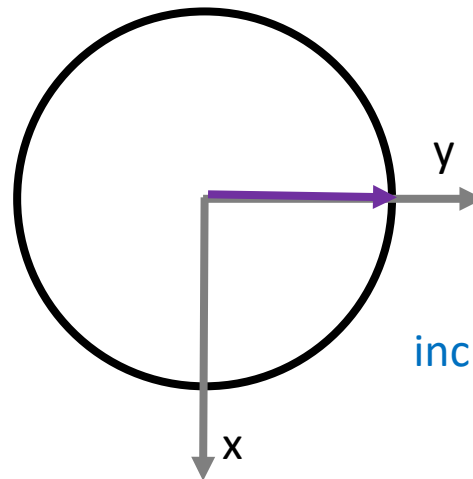
$$DR = \frac{\text{Range} \uparrow}{\text{Sensitivity} \uparrow}$$

Dynamic range  
remains the same:  
Trade-off

$B \propto \text{spin phase} \propto \text{area}$

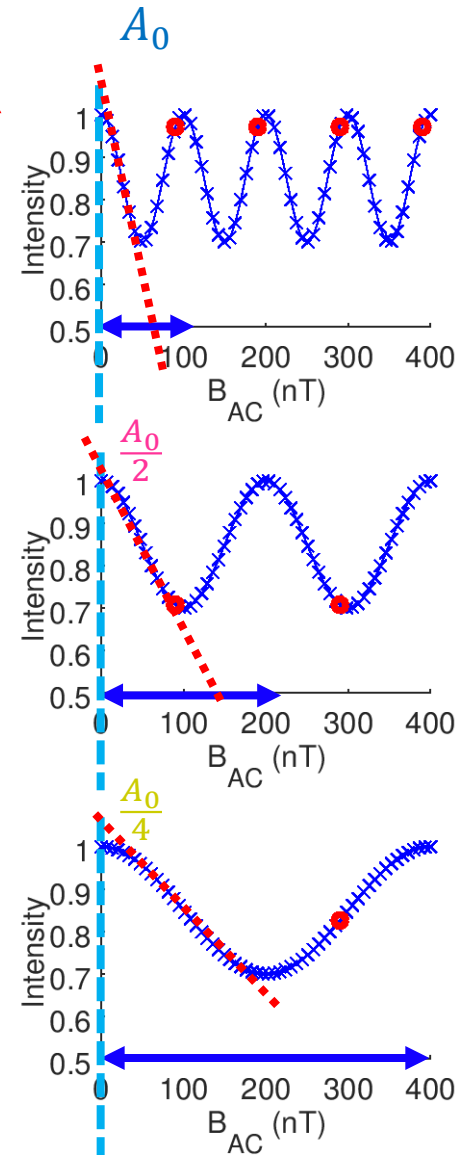


- Essentially, Hahn-echo measures the area
- Decrease the measured area
  - Period of the magnetic field increases



Range  
increases

Sensitivity improves

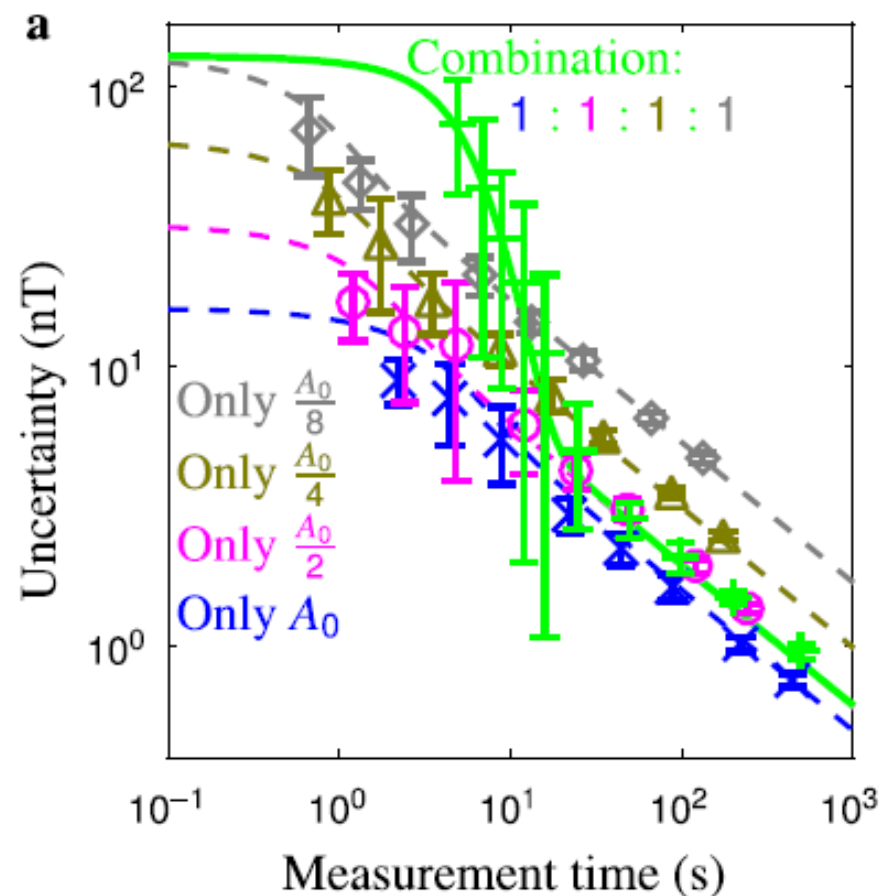
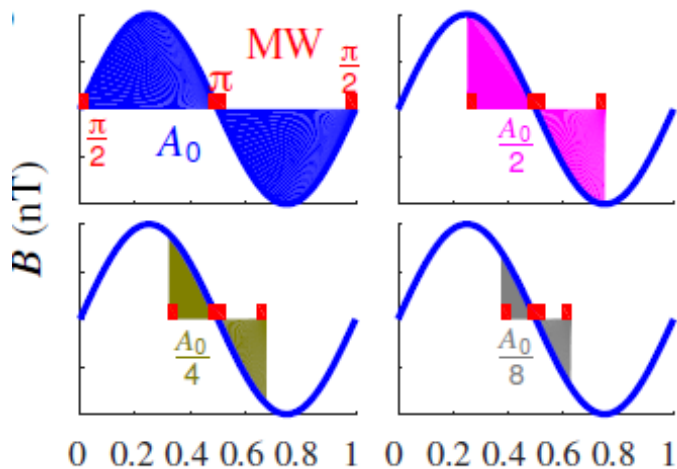


# High dynamic range retaining its sensitivity

## Our idea

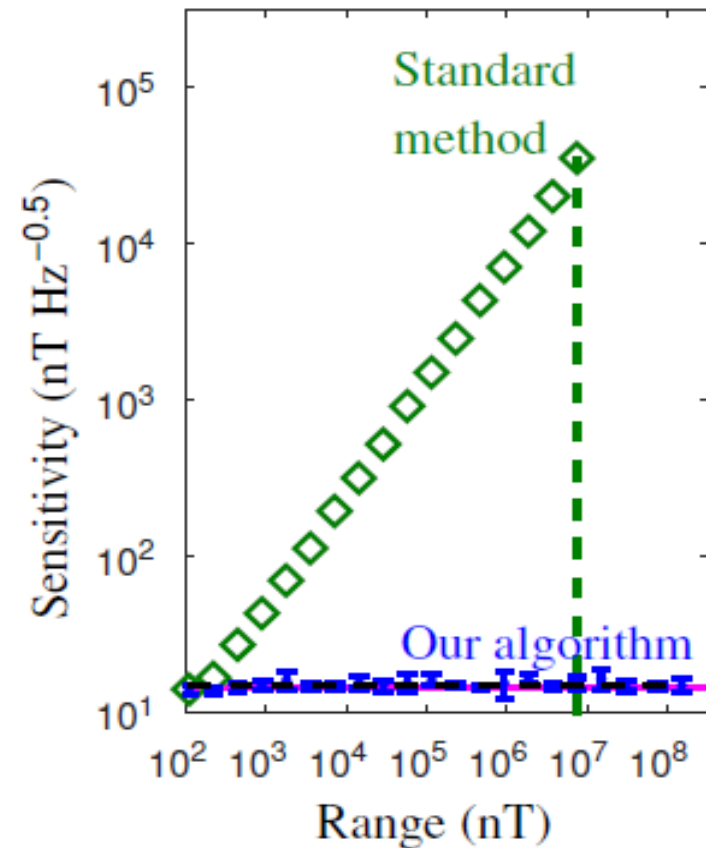
- Change of the pulse interval and combine different sequences of area ( $A_n$ ).
- Calculation of the optimal with an algorithm based on
- Calculation of the optimum measurement time.

## Results



Algorithm: The measurement resulting from different areas combined via Bayes' theorem.

Dynamic range of about  $10^7$  retaining high sensitivity. Two orders of magnitude over the previous best (Bonato et al., *Nat. Nanotechnol.*, 11, 247 (2015)).

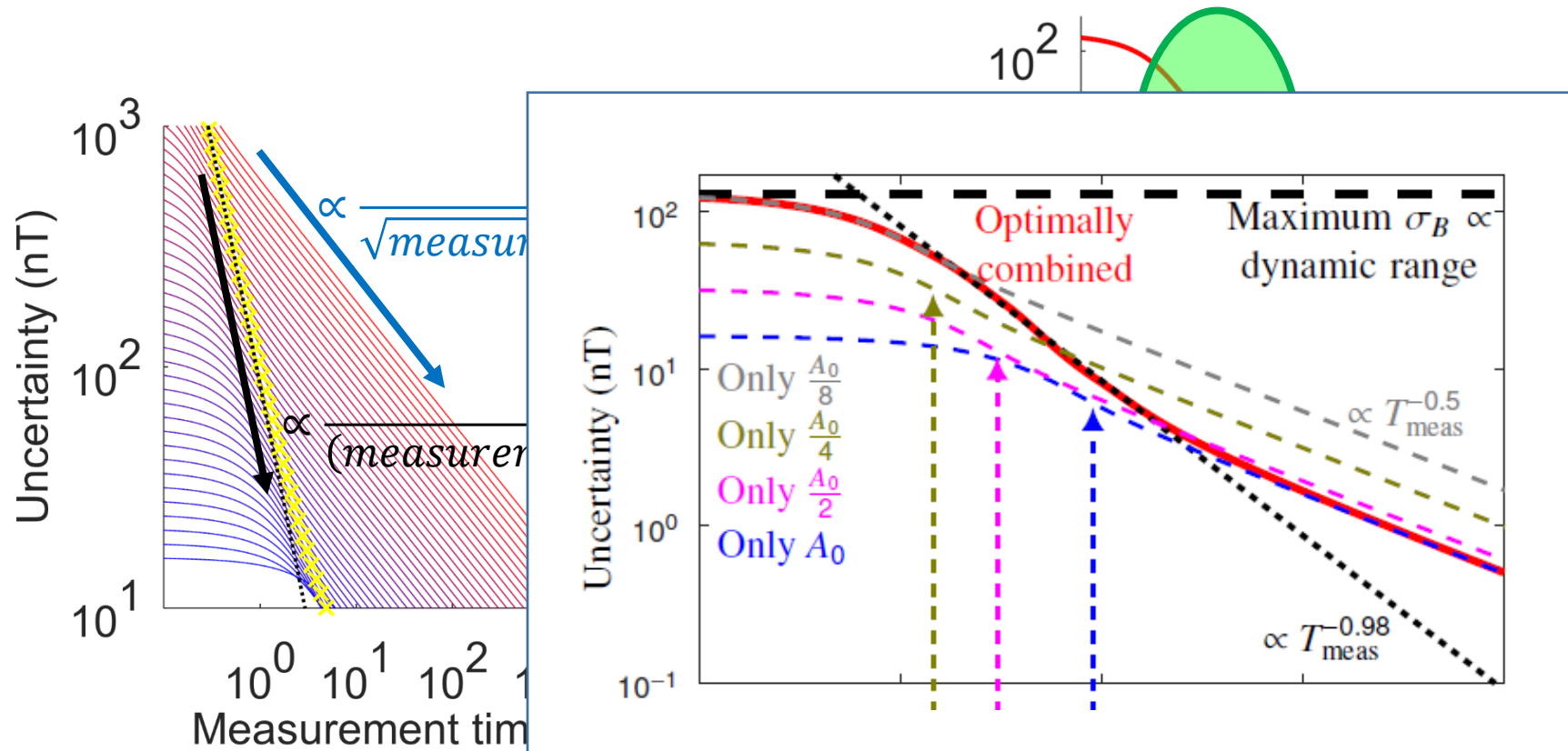


Applicable for other modulo-limited sensors. Important for entanglement-based sensors.

The enhancement of dynamic range will lead to expanding the area of the measurement space.

# Algorithm – scaling: time dependence

steep region



We showed the mechanism of Heisenberg-like scaling ( $T^{-2}$ ).

# Short Summary of last part

- Dynamic range of about  $10^7$  retaining high sensitivity was demonstrated. Two orders of magnitude over the previous best.
- Applicable for other modulo-limited sensors. Important for entanglement-based sensors.
- The enhancement of dynamic range will lead to expanding the area of the measurement space.
- We showed the mechanism of Heisenberg-like scaling ( $T^{-2}$ ).

"Ultra-high dynamic range quantum measurements retaining its sensitivity",

E. D. Herbschleb, H. Kato, T. Makino, S. Yamasaki, N. Mizuochi,  
*Nature Communications*, 12, 306 (2021)

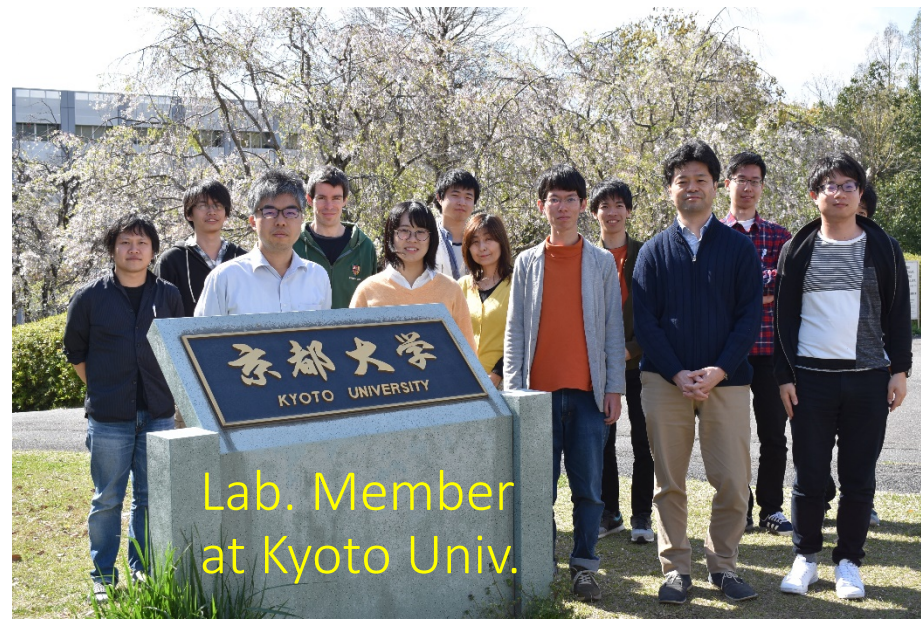
- Dr. S. Yamasaki, Dr. H. Kato, Dr. T. Makino, Dr. Matsuzaki, and group members (AIST)
- Prof. M. Hatano (Univ. of Tokyo Inst. Tech.)
- Dr. T. Taniguchi (NIMS)
- Prof. H. Kosaka (Yokohama Univ.)
- Dr. K. Semba, (NICT)
- Dr. Saito, Dr. Munro, Dr. Yamaguchi (NTT)
- Prof. K. Nemoto (NII)
- Prof. Y. Suzuki and group members (Osaka Univ.)
- Prof. N. Tokuda (Kanazawa Univ.)
- Prof. J. Wrachtrup and group members (Stuttgart Univ.)
- Prof. F. Jelezko (Ulm Univ.)
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Dr. Ohki, Dr. Hayashi



Q-LEAP



Lab. Member  
at Kyoto Univ.

1. Overview: Quantum sensor, NV center in diamond
2. Characteristics of NV centers for sensor  
     $\sim$  Why can we improve sensitivity and spatial resolution?  $\sim$
3. How to measure? (Magnetic field, electric field, temperature)
4. Expected applications
5. Our recent studies